Package: TFunHDDC (via r-universe)

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 $contaminated Triangles \quad contaminated Triangles$

Description

Simulated triangle data produced as an example of mild contaminated data with behavioural outliers.

Value

fd A functional data object representing the fitted triangle data.

groupd Group classifications for each curve as a ordinary behavioral group (1,2,3, or 4)

or outlier (4 as outliers to group 1 and 6 as outliers for group 3).

Author(s)

Cristina Anton and Iain Smith

References

- Cristina Anton, Iain Smith Model-based clustering of functional data via mixtures of t distributions. Advances in Data Analysis and Classification (to appear).

fitNOxBenchmark fitNOxBenchmark

Description

Extract NOx data from fda.usc

Usage

fitNOxBenchmark(nbasis=15)

Arguments

nbasis The number of basis functions to fit to the simulated data.

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Details

Open NOx data from the poblenou data set of fda.usc. Fit the data to a given number of basis functions and adjust classes for festive days into just weekdays and weekends.

Value

fd A functional data object representing the fitted NOx data.

groupd Group classifications for each curve as a curve representing a weekday or week-

end/festive day.

Author(s)

Cristina Anton and Iain Smith

References

- Febrero-Bande M, Galeano P, Gonz~alez-Manteiga W (2008) Outlier detection in functional data by depth measures, with application to identify abnormal nox levels. Environmetrics 19:331-345. <//doi.org/10.1002/env.878>.
- Cristina Anton, Iain Smith Model-based clustering of functional data via mixtures of t distributions. Advances in Data Analysis and Classification (to appear).

See Also

plotN0x

Examples

Univariate Contaminated Data
data1<-fitNOxBenchmark(15)
plotNOx(data1)</pre>

genModelFD

genModelFD

Description

Generate functional data with coefficients distributed according to a finite mixture of contamined normal distributions such that for the *k*th cluster we have the multivariate contaminated normal distribution with density

$$f(\gamma_i; \theta_k) = \alpha_k \phi(\gamma_i; \mu_k, \Sigma_k) + (1 - \alpha_k) \phi(\gamma_i; \mu_k, \eta_k \Sigma_k)$$

where $\alpha_k \in (0.5, 1)$ represents the proportion of uncontaminated data, $\eta_k > 1$ is the inflation coefficient due to outliers, and $\phi(\gamma_i; \mu_k, \Sigma_k)$ is the density for the multivariate normal distribution $N(\mu_k, \Sigma_k)$.

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Usage

Arguments

ncurves The number of curves total for the simulation.

nsplines The number of splines to fit to the simulated data.

alpha The proportion of uncontaminated data in each group.

eta The inflation coefficient that measures the increase in variability due to the out-

liers.

Details

The data are generate from the model $FCLM[a_k, b_k, \mathbf{Q}_k, d_k, \alpha_k, \eta_k]$. The number of clusters is fixed to K=3 and the mixing proportions are equal $\pi_1=\pi_2=\pi_3=1/3$. We consider the following values of the parameters

```
Group 1:d = 5, a = 150, b = 5, \mu = (1, 0, 50, 100, 0, ..., 0)
Group 2: d = 20, a = 15, b = 8, \mu = (0, 0, 80, 0, 40, 2, 0, ..., 0)
Group 3: <math>d = 10, a = 30, b = 10, \mu = (0, ..., 0, 20, 0, 80, 0, 0, 100),
```

where d is the intrinsic dimension of the subgroups, μ is the mean vector of size 70, a is the values of the d-first diagonal elements of \mathbf{D} , and b the value of the last 70-d- elements. Curves as smoothed using 35 Fourier basis functions.

Value

fd A functional data object representing the simulated data.

groupd Group classifications for each curve.

Author(s)

Cristina Anton and Iain Smith

References

- Amovin-Assagba M, Gannaz I, Jacques J (2022) Outlier detection in multivariate functional data through a contaminated mixture model. Comput Stat Data Anal 174. - Cristina Anton, Iain Smith Model-based clustering of functional data via mixtures of t distributions. Advances in Data Analysis and Classification (to appear).

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genTriangles

genTriangles

Description

Generate contaminated triangle data. Groups 1, 2, 3, and 4 are separable over the two dimensions of functional data. Groups 5 and 6 contain the contaminated curves of groups 1 and 3 respectively.

Usage

genTriangles()

Details

Group 1:

$$X_1(t) = U + (0.6 - U)H_1(t) + \epsilon_1(t)$$

$$X_2(t) = U + (0.5 - U)H_1(t) + \epsilon_1(t)$$

Contaminated
$$X_1(t) = \sin(t) + (0.6 - U)H_1(t) + \epsilon_2(t)$$

Contaminated
$$X_2(t) = \sin(t) + (0.5 - U)H_1(t) + \epsilon_2(t)$$

Group 2:

$$X_1(t) = U + (0.6 - U)H_2(t) + \epsilon_1(t)$$

$$X_2(t) = U + (0.5 - U)H_2(t) + \epsilon_1(t)$$

Group 3:

$$X_1(t) = U + (0.5 - U)H_1(t) + \epsilon_1(t)$$

$$X_2(t) = U + (0.6 - U)H_2(t) + \epsilon_1(t)$$

Contaminated
$$X_1(t) = \sin(t) + (0.5 - U)H_1(t) + \epsilon_3(t)$$

Contaminated
$$X_2(t) = \sin(t) + (0.6 - U)H_2(t) + \epsilon_3(t)$$

Group 4:

$$X_1(t) = U + (0.5 - U)H_2(t) + \epsilon_1(t)$$

 $X_2(t)=U+(0.6-U)H_1(t)+\epsilon_1(t)$. Here $t\in[1,21]$, $H_1(t)=(6-|t-7|)_+$, and $H_2(t)=(6-|t-15|)_+$, with $(\cdot)_+$ representing the positive part. $U\sim\mathcal{U}(0,0.1)$, and $\epsilon_1(t)\sim N(0,0.5)$, $\epsilon_2(t)\sim N(0,2)$, $\epsilon_3(t)\sim Cauchy(0,4)$ are mutually independent white noises and independent of U. We simulate 100 curves for each group, groups 1 and 3 consisting of 80 ordinary curves and 20 contaminated curves. Curves are smoothed using a 25 cubic B-spline basis.

Value

fd List of functional data objects representing the two dimensions of triangle data.

groupd Group classification for each curve

Author(s)

Cristina Anton and Iain Smith

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References

- C.Bouveyron and J.Jacques (2011), Model-based Clustering of Time Series in Group-specific Functional Subspaces, Advances in Data Analysis and Classification, vol. 5 (4), pp. 281-300, <doi:10.1007/s11634-011-0095-6>
- Schmutz A, Jacques J, Bouveyron C, et al (2020) Clustering multivariate functional data in group-specific functional subspaces. Comput Stat 35:1101-1131
- Cristina Anton, Iain Smith Model-based clustering of functional data via mixtures of t distributions. Advances in Data Analysis and Classification (to appear).

See Also

```
plotTriangles
```

Examples

```
# Multivariate Contaminated Triangles
conTrig <- genTriangles()
cls = conTrig$groupd
plotTriangles(conTrig)</pre>
```

plotN0x

plotNOx

Description

Plot data returned by fitN0xBenchmark as lines coloured according to the assigned clusters.

Usage

```
plotN0x(fdn)
```

Arguments

fdn

List with an element fd given the functional data, and an element groupd given the classes; usually returned from the function fitNOxBenchmark.

Value

No return value, used for side effects.

Author(s)

Cristina Anton and Iain Smith

See Also

fitN0xBenchmark

plotTriangles 7

Examples

```
# Univariate Contaminated Data
data1<-fitNOxBenchmark(15)
plotNOx(data1)</pre>
```

plotTriangles

plotTriangles

Description

Plot data returned by genTriangles as lines coloured according to the assigned clusters.

Usage

```
plotTriangles(fdt)
```

Arguments

fdt

List with an element fd given the functional data, and an element groupd given the classes, as returned from the function <code>genTriangles</code>.

Value

No return value, used for side effects.

Author(s)

Cristina Anton and Iain Smith

See Also

```
genTriangles
```

```
conTrig <- genTriangles()
plotTriangles(conTrig)</pre>
```

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predict.tfunHDDC

predict.tfunHDDC: Predicting Function for t-funHDDC Objects

Description

Provides the matrix of classification probabilities and the classification vector for inputted observations assuming the model provided by the tfunHDDC object.

Usage

```
## S3 method for class 'tfunHDDC'
predict(object, data=NULL, ...)
```

Arguments

object An object of class tfunHDDC

data Data frame (univariate funtional data) or a list (multivariate functional data) of

new observations on the same variables used in the fitting of the tfunHDDC object. If NULL, then the observations used in the fitting of the tfunHDDC object are

inputted.

... Arguments to be passed to other functions.

Value

t Matrix of classification probabilities

class Vector of maximum a posteriori classifications

Author(s)

Cristina Anton, Iain Smith

References

-Andrews JL, McNicholas PD (2012) Model-based clustering, classi

cation, and discriminant analysis via mixtures of multivariate t-distributions: The teigen family. Stat Comput 22:10211029. <doi.org/10.1007/ s11222-011-9272-x>

-Andrews JL, Wickins JR, Boers NM, et al (2018) An R package for modelbased clustering and classi

cation via the multivariate t distribution. Journal of Statistical Software 83(7):1-32

- Cristina Anton, Iain Smith Model-based clustering of functional data via mixtures of t distributions. Advances in Data Analysis and Classification (to appear).

See Also

tfunHDDC

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```
set.seed(1027)
#simulataed univariate data
data = genModelFD(ncurves=300, nsplines=35, alpha=c(0.9,0.9,0.9),
                  eta=c(10, 7, 17))
plot(data$fd, col = data$groupd)
clm = data$groupd
model1=c("AkjBkQkDk", "AkjBQkDk", "AkBkQkDk", "ABkQkDk", "AkBQkDk", "ABQkDk")
###################classification example with predictions
training=c(1:50,101:150, 201:250)
test=c(51:100,151:200, 251:300)
known1=clm[training]
t4<-tfunHDDC(data$fd[training], K=3, threshold=0.2, init="kmeans", nb.rep=1,
             dfconstr="no", dfupdate="numeric", model=model1[1],known=known1,
             itermax = 10)
if (!is.null(t4$class)) {
 table(clm[training], t4$class)
 p1<-predict.tfunHDDC(t4,data$fd[test] )</pre>
 if (!is.null(p1$class)) table(clm[test], p1$class)
####################NOX data
data1=fitNOxBenchmark(15)
plotN0x(data1)
###example for prediction
training=c(1:50)
test=c(51:115)
known1=data1$groupd[training]
t1<-tfunHDDC(data1$fd[training],K=2,threshold=0.6,init="kmeans",nb.rep=10,
             dfconstr="no", model=c("AkjBkQkDk", "AkjBQkDk", "AkBkQkDk",
             "ABkQkDk", "AkBQkDk", "ABQkDk"), known=known1)
if (!is.null(t1$class)) {
```

```
table(data1$groupd[training], t1$class)
p1<-predict.tfunHDDC(t1,data1$fd[test] )
if (!is.null(p1$class)) table(data1$groupd[test], p1$class)
}</pre>
```

tfunHDDC

tfunHDDC: Function for Model-Based Clustering of Functional Data with Outliers Using the t-Distribution.

Description

tfunHDDC is an adaptation of funHDDC (Schmutz et al., 2018) that uses t-distributions for robust clustering in the presence of outliers.

Usage

Arguments

1	Sumenes	
	data	In the univariate case: a functional data object produced by the fda package. In the multivariate case: a list of functional data objects.
	K	The number of clusters or list of clusters to try, for example K=2:10.
	dfstart	The df (degrees of freedom) to which we initialize the t-distribution.
	dfupdate	Either "numeric", or "approx". The default is "approx" indicating a closed form approximation be used. Alternatively, "numeric" can be specified which makes use of uniroot.
	dfconstr	"yes" when df (degrees of freedom) for the t-distribution should be the same between all clusters; "no" when df may be different between clusters.
	model	The chosen model among 'AkjBkQkDk', 'AkjBQkDk', 'AkBkQkDk', 'ABkQkDk', 'AkBQkDk', 'AkBQkDk'. 'AkjBkQkDk' is the default. We can test multiple models at the same time with the command c(). For example c("AkjBkQkDk","AkjBQkDk").
	threshold	The threshold of the Cattell' scree-test used for selecting the group-specific intrinsic dimensions.
	known	A vector of known classifications that can be numeric or NA. It is optional for clustering. For classification, curves with unknown classification should be

given the value NA within known (see the examples below). Must be the same

length as the number of curves in the data set.

itermax The maximum number of iterations.

eps The threshold of the convergence criterion.

init A character string. It is the way to initialize the EM algorithm. There are

five ways of initialization: "kmeans" (default), "param", "random", "mini-em", "vector", or "tkmeans". See details for more information. It can also be directly

initialized with a vector containing the prior classes of the observations.

criterion The criterion used for model selection: bic (default) or icl.

d_select "Cattell" (default), "BIC", or "grid". This parameter selects which method to

use to select the intrinsic dimensions of subgroups. "grid" will select d based on the criterion value after running each combination of d1, d2, ..., dK for the groups. d used for each group is based on the values for d_range. "grid" will only work for a single value of K (not a list). See details for more information.

init.vector A vector of integers or factors. It is a user-given initialization. It should be of

the same length as of the data. Only used when init="vector".

show Use show = FALSE to settle off the informations that may be printed.

mini.nb A vector of integers of length two. This parameter is used in the "mini-em"

initialization. The first integer sets how many times the algorithm is repeated; the second sets the maximum number of iterations the algorithm will do each time. For example, if init="mini-em" and mini.nb=c(5,10), the algorithm will be launched 5 times, doing each time 10 iterations; finally the algorithm will begin

with the initialization that maximizes the log-likelihood.

min.individuals

This parameter is used to control for the minimum population of a class. If the population of a class becomes stricly inferior to 'min.individuals' then the algorithm stops and gives the message: 'pop<min.indiv.'. Here the meaning of "population of a class" is the sum of its posterior probabilities. The value of

'min.individuals' cannot be lower than 2.

mc.cores Positive integer, default is 1. If mc.cores>1, then parallel computing is used,

using mc.cores cores. Warning for Windows users only: the parallel computing can sometimes be slower than using one single core (due to how parLapply

works).

nb. rep A positive integer (default is 1 for kmeans initialization and 20 for random ini-

tialization). Each estimation (i.e. combination of (model, K, threshold)) is repeated nb.rep times and only the estimation with the highest log-likelihood is

kept.

keepAllRes Logical. Should the results of all runs be kept? If so, an argument all_results is

created in the results. Default is TRUE.

kmeans.control A list. The elements of this list should match the parameters of the kmeans ini-

tialization (see kmeans help for details). The parameters are "iter.max", "nstart" and "algorithm". "alpha" is an added parameter for the tkmeans initialization

(see tkmeans help for details)

d_max A positive integer. The maximum number of dimensions to be computed. De-

fault is 100. It means that the instrinsic dimension of any cluster cannot be larger than d_max. It quickens a lot the algorithm for datasets with a large number of

variables (e.g. thousands).

d_range Vector of values to use for the intrinsic dimension for each group when d_select="grid".

verbose Whether to print progress and approximate timing information as tfunHDDC ex-

ecutes. TRUE (default when running in serial) or FALSE (default when running parallel).

Details

If we choose init="random", the algorithm is run 20 times with the same model options and the solution which maximises the log-likelihood is printed. This explains why sometimes with this initialization it runs a bit slower than with 'kmeans' initialization.

If the warning message: "In tfunHDDC(...): All models diverged" is printed, it means that the algorithm found less classes that the chosen number (parameter K). Because the EM algorithm is used, it could be because of a bad initialization of the EM algorithm. So we have to restart the algorithm multiple times in order to check if with a new initialization of the EM algorithm the model converges, or if there is no solution with the chosen number K.

The different initializations are:

"mini-em": it is an initialization strategy for which the classes are randomly initialized and the EM algorithm is run for several iterations. This action is repetead a few times (the default is 5 iterations and 10 times). At the end, the initialization chosen is the one which maximise the log-likelihood (see mini.nb for more information about its parameters).

"random": the classes are randomly given using a multinomial distribution

"kmeans": the classes are initialized using the kmeans function (with algorithm="Hartigan-Wong"; nstart=4; iter.max=50); note that the user can use his own arguments for kmeans using the dot-dot-dot argument

"tkmeans": the classes are initialized using the tkmeans function (with same default initialization as kmeans); note that the user can use his own arguments for tkmeans using the dot-dot-dot argument

A prior class "vector": It can also be directly initialized with a vector containing the prior classes of the observations. To do so use init="vector" and provide the vector in the argument init.vector.

Note that the BIC criterion used in this function is to be maximized and is defined as 2*LL-k*log(n) where LL is the log-likelihood, k is the number of parameters and n is the number of observations.

There are three methods for selecting the intrinsic dimension using d_select:

"Cattell": Runs a Cattell's scree test to approximate the intrinsic dimension that yields the greatest improvement in clustering.

"BIC": At each iteration we tests each value for each group's intrinsic dimension and sets the intrinsic dimension that yields the best BIC.

"grid": Runs every combination of hyperparameters (eg. K=2, threshold = 0.05, model = ...) for every combination of intrinsic dimensions that can be set with the given d_range (with K=2 and d_range = c(2, 10) it would set (2,2), (2, 10), (10, 2), and (10, 10)). Due to the sharp increase in test cases it is recommended that this mode is run in parallel if possible. Doing an intial short run to approximate the timing with verbose = TRUE is suggested as well.

Value

d The number of dimensions for each cluster.

a Values of parameter a for each cluster.

b Values of parameter b for each cluster.

mu The mean of each cluster in the original space.

prop The proportion of individuals in each cluster.

loglik The maximum of log-likelihood.
loglik_all The log-likelihood at each iteration.

posterior The posterior probability for each individual to belong to each cluster.

class The clustering partition.

BIC The BIC value.

ICL The ICL value.

complexity the number of parameters that are estimated.

all_results if multiple number of clusters or models are considered, results for each model

are stored here

nux Values for the degrees of freedom of the t-distributions for each group.

Author(s)

Cristina Anton, Iain Smith, and Malcolm Nielsen

References

- Andrews JL and McNicholas PD. "Model-based clustering, classification, and discriminant analysis with the multivariate *t*-distribution: The *t*EIGEN family" *Statistics and Computing* 22(5), 1021–1029.
- Andrews JL, McNicholas PD, and Subedi S (2011) "Model-based classification via mixtures of multivariate t-distributions" *Computational Statistics and Data Analysis* 55, 520–529.
- C.Bouveyron and J.Jacques, Model-based Clustering of Time Series in Group-specific Functional Subspaces, Advances in Data Analysis and Classification, vol. 5 (4), pp. 281-300, 2011 <doi:10.1007/s11634-011-0095-6>
- Schmutz A, Jacques J, Bouveyron C, et al (2020) Clustering multivariate functional data in group-specific functional subspaces. Comput Stat 35:1101-1131
- Cristina Anton, Iain Smith Model-based clustering of functional data via mixtures of t distributions. Advances in Data Analysis and Classification (to appear).

See Also

```
teigen, kmeans, tkmeans, predict.tfunHDDC
```

```
plot(data$fd, col = data$groupd)
clm = data$groupd
model1=c("AkjBkQkDk", "AkjBQkDk", "AkBkQkDk", "ABkQkDk", "AkBQkDk", "ABQkDk")
t1<-tfunHDDC(data$fd,K=3,threshold=0.2,init="kmeans",nb.rep=1,dfconstr="no",
             dfupdate="numeric", model=model1[1], itermax=10)
if (!is.null(t1$class)) table(clm, t1$class)
############example when some classifications are known
known1=rep(NA,1,300)
known1[1]=clm[1]
known1[103]=clm[103]
known1[250]=clm[250]
t2<-tfunHDDC(data$fd,K=3,threshold=0.2,init="kmeans",nb.rep=1,dfconstr="no",
             \label{local_def} \mbox{\tt dfupdate="numeric", model=model1[1],known=known1, itermax=10)}
if (!is.null(t2$class)) table(clm, t2$class)
###### example when some classifications are known
known1=rep(NA,1,300)
known1[1:100]=rep(3,1,50)
t3<-tfunHDDC(data$fd,K=3,threshold=0.2,init="kmeans",nb.rep=1,dfconstr="no",
             dfupdate="numeric", model=model1[1],known=known1, itermax=10)
if (!is.null(t3$class)) table(clm, t3$class)
#########################multivariate simulated data
set.seed(1027)
conTrig <- genTriangles()</pre>
cls = conTrig$groupd # groups 5 and 6 (contaminated) into 1 and 3 respectively
res_s = tfunHDDC(conTrig$fd, K=4, dfconstr="no", dfupdate="numeric",
                 model="ABKQKDK", init="kmeans", threshold=0.2, nb.rep=1,
                 itermax=10)
if (!is.null(res_s$class)) table(cls, res_s$class)
```

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